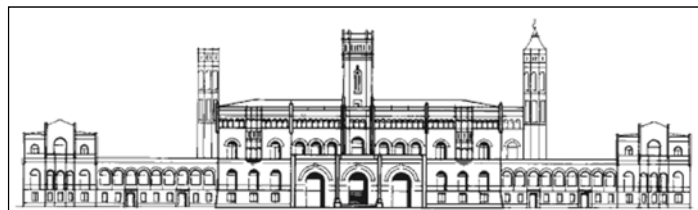


Bachelor programme Mathematics
Master programme Mathematics

Module catalogue

As at 31.10.2016

Faculty of Mathematics and Physics
of the Leibniz University Hannover



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Preface

The module catalogue mathematics consist of two parts, the module descriptions and the appendix with the course descriptions. Given that different courses can be chosen for elective module, these will be described in more detail in the appendix. In those cases the information of the course overview and the frequency of the course are found at the courses and not at the modules.

Please note that this here is a compilation of the courses of the mathematics that are offered on a regular basis. In particular further courses of the university calender" can be assigned to "compulsory elective module and den Elective module.

The module catalogue should also be understood as addition to the Examination regulations. The recent version of our Examination regulations can be found under

<http://www.uni-hannover.de/de/studium/studiengaenge/mathe/ordnungen/index.php>

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Studienverlaufsplan

	1. Semester	2. Semester	3. Semester	4. Semester	5. Semester	6. Semester	LP
Basics	Analysis I 10 LP, SL, PL	Analysis II 10 LP, SL, PL	(Analysis III 10 LP, SL, PL)	Probability and Statistics I 10 LP, SL, PL	Analysis III 10 LP, SL, PL		84
	Lineare Algebra I 10 LP, SL, PL	Lineare Algebra II 10 LP, SL, PL	Algebra I 10 LP, SL, PL				
			Numerical Mathematics I 10 LP, SL, PL				
			Algorithmic programming 4 LP, PL				
Key skills			Seminar 5 LP, SL				5
Proseminar			Proseminar 5 LP, PL				5
optional section			courses in an extent of 40 CP, 4xSL, 4xPL				40
Computer Science			Basics of theoretical Informatics 5 CP, SL, PL		Datenstrukturen und Algorithmen 5 CP, SL, PL		10
application subject	application subjects are: business administration, Geodesy and Geoinformatics, Informatics, Philosophy, Physics and Economics. Other subjects are possible upon request. 18 CP						18
Seminar					Seminar 5 CP, PL		5
Bachelor thesis						Bachelorthesis 13 CP	13

Credit points	20/2	20/2	According to individual planning variable	180
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Modules of Bachelor Mathematics

Compulsory module Bachelor

Module name, Nr.	Analysis I	0201
Regularity	wintersemester, annually	
Responsibility of module	Institut für Analysis und Institut für Angewandte Mathematik	
Type of Course (SWS)	lecture „Analysis I“ (4 SWS) tutorial on „Analysis I“ (2 SWS)	
Major course assessment for acquisition of LP	Course achievement: Tutorial Examination performance: Exam	
Grade composition	Grade of exam	
Credit points (ECTS):	10	Presence study (h): 90 Self-study (h): 210
Learning outcomes: Competence in dealing with mathematical language. Basic understanding of the correct solution of mathematical problems by means of one-dimensional convergence considerations, differential and integral calculus. As a result of the exercise sessions, the students are familiar with mathematically exact formulations and conclusions in simple contexts and are able to present them.		
Course overview: <ul style="list-style-type: none"> • Number systems; systematic introduction of real numbers • Sequences and series • Convergence and continuity • Differential calculus for functions of one variable • Integral calculus for functions of one variable. 		
Reading list: <ul style="list-style-type: none"> 📖 H. Amann & J. Escher: <i>Analysis I</i>, Birkhäuser Verlag, 2002 📖 O. Forster: <i>Analysis 1</i>, Vieweg+Teubner 2008 📖 K. Königsberger: <i>Analysis 1</i>, Springer Verlag 2004 		
Recommended previous knowledge: School knowledge in Mathematics (gymnasiale Oberstufe)		
if applicable entrance requirement and if applicable restriction of participants:		
Applicability: <ul style="list-style-type: none"> • Bachelor programme Mathematics • Fächerübergreifender Bachelorstudiengang 		

Module name, Nr.	Analysis II	0202
Regularity	Sommersemester, annually	
Responsibility of module	Institut für Analysis und Institut für Angewandte Mathematik	
Course(SWS)	lecture „Analysis II“ (4 SWS) tutorial on „Analysis II“ (2 SWS)	
Major course assessment for acquisition of LP	Course achievement: Tutorial Examination performance: Exam	
Grade composition	Grade of exam	
Credit points (ECTS):	10	Presence study (h): 90 Self-study (h): 210

Learning outcomes:

Basic understanding of the correct solution of mathematical and natural sciences tasks using multidimensional convergence considerations, differential and integral calculus. Secure mastery of the appropriate techniques and mathematical methods of proof. Teamwork by handling tasks in groups and discussing them in the exercise sessions.

Course overview:

- Topological concepts such as metric and normed spaces, convergence, continuity, completeness, compactness;
- Differentiation of functions of several variables, total and partial differentiability, theorems on inverse functions and implicit functions, local extrema with and without constraints; vector fields and potentials;
- Ordinary differential equations, existence, uniqueness, elementary methods of solution.

Reading list:

- 📖 H. Amann & J. Escher: *Analysis II*, Birkhäuser Verlag, 1999
- 📖 O. Forster: *Analysis 2*, Vieweg+Teubner, 2006
- 📖 J. Jost: *Postmodern Analysis*, Springer Verlag 2005
- 📖 K. Königsberger: *Analysis 2*, Springer Verlag 2004

Recommended previous knowledge:

- Linear Algebra I
- Analysis I

if applicable entrance requirement and if applicable restriction of participants:

Applicability:

- Bachelor programme Mathematics
- **Fächerübergreifender Bachelorstudiengang**

Module name, Nr.	Advanced Analytic Methods (Fortgeschrittene analytische Methoden)		0203
Regularity	wintersemester, annually		
Responsibility of module	Institut für Analysis und Institut für Angewandte Mathematik		
Course(SWS)	lecture „Analysis III“ (4 SWS) tutorial on „Analysis III“ (2 SWS)		
Major course assessment for acquisition of LP	Course achievement: Tutorial Examination performance: Exam or oral examination		
Grade composition	Grade of exam or oral examination		
Credit points (ECTS):	10	Presence study (h):	90
		Self-study (h):	210
Learning outcomes:	Deepened understanding of analytical methods, especially in the theory of measures and integration as well as vector analysis. Ability to independently elaborate more difficult mathematical arguments on topics of the lecture and their presentation in the exercise groups.		
Course overview:	Elements of Lebesgue's measure theory, multidimensional Lebesgue integral along with essential theorems (monotone and dominated convergence, Fubini's theorem, transformation rule); vector calculus; Gauss' and Stokes' theorems; manifolds.		
Reading list:	<ul style="list-style-type: none"> • H. Amann & J. Escher: <i>Analysis III</i> 📖 W. M. Boothby: <i>An introduction to differentiable manifolds and Riemannian geometry</i>, Academic Press 📖 O. Forster: <i>Analysis 3</i>, Vieweg+Teubner, 2008 📖 J. Jost: <i>Postmodern Analysis</i>, Springer Verlag 2005 		

Recommended previous knowledge:

- Analysis I + II




if applicable entrance requirement and if applicable restriction of participants:

Applicability:


- Bachelor programme Mathematics




Module name, Nr.	Algebraic methods I (Algebraische Methoden I)		0101
Regularity	Wintersemester, annually		
Responsibility of module	Institut für Algebra, Zahlentheorie und Diskrete Mathematik und Institut für Algebraische Geometrie		
Course(SWS)	lecture „Lineare Algebra I“ (4 SWS) tutorial on „Lineare Algebra I“ (2 SWS)		
Major course assessment for acquisition of LP	The Course achievement is to be performed at the tutorial to „Lineare Algebra I“. Examination performance: Exam for „Lineare Algebra I“		
Grade composition	Grade of exam		
Credit points (ECTS):	15	Presence study (h):	135 Self-study (h): 315
Learning outcomes: Basic understanding of the mathematical way of thinking and its application towards a variety of problems. Solid competence in handling systems of linear equations and the corresponding methods for solving them; sound knowledge of the underlying algebraic structures. Capability of expressing and presenting mathematical reasoning, and knowledge of adequate methods for this.			
Course overview: Linear Algebra I: <ul style="list-style-type: none"> • Basic properties of vector spaces (basis and dimension); • linear maps and matrices; • determinants; • systems of linear equations and methods for solving them (Gauss algorithm); • eigenvalues and eigenvectors; • diagonalisation. 			
Reading list: 📖 Linear Algebra I: G. Fischer: <i>Lineare Algebra</i>			
Recommended previous knowledge: 📖 School knowledge in Mathematics (gymnasiale Oberstufe)			
if applicable entrance requirement and if applicable restriction of participants:			
Applicability: <ul style="list-style-type: none"> • Bachelor programme Mathematics • As module Lineare Algebra I also for: Fächerübergreifender Bachelorstudiengang 			

Module name, Nr.	Key competence: Computeralgebra	???
Regularity	Wintersemester, annually	
Responsibility of module	Institut für Algebra, Zahlentheorie und Diskrete Mathematik und Institut für Algebraische Geometrie	
Course(SWS)	Practical course „Computeralgebra“ (3 SWS)	
Major course assessment for acquisition of LP	Course achievement at university lecturer's option	
Grade composition		

Credit points (ECTS):	5	Presence study (h):	60	Self-study (h):	90
Learning outcomes:					
Experience in appropriate use of computer algebra systems as tools for solving problems from Analysis and Linear Algebra; in particular: choice of appropriate tools, knowing and avoiding potential mistakes, knowing the limits of such systems, use of visualization tools and programming of smaller functions/methods/procedures.					
Course overview:					
<ul style="list-style-type: none"> • Basic knowledge on the functioning and use of computer algebra systems • Selected applications from Linear Algebra, e.g. solving linear systems of equations, linear maps, change of basis • Selected applications from Analysis, e.g. zeros, differentiation, visualization of graphs of functions • Selected applications to topics known from school: gcd, conic sections • Small projects, e.g. solutions of polynomial equations with visualization, Chinese Remainder Theorem 					
Reading list:					
 T. Theobald, S. Ilman: Einführung in die Computerorientierte Mathematik, Springer Spektrum 2015					
Recommended previous knowledge:					
 Lineare Algebra, Analysis  Some basic experience in the use of computers					
if applicable entrance requirement and if applicable restriction of participants:					
Applicability:					
<ul style="list-style-type: none"> • Bachelor programme Mathematics 					

Module name, Nr.	Algebraic methods II (Algebraische Methoden II)			0102	
Regularity	Sommersemester, annually				
Responsibility of module	Institut für Algebra, Zahlentheorie und Diskrete Mathematik und Institut für Algebraische Geometrie				
Course(SWS)	lecture „Lineare Algebra II“ (4 SWS) Tutorial zu „Lineare Algebra II“ (2 SWS)				
Major course assessment for acquisition of LP	The Course achievement is to be performed at the tutorial Examination performance: Exam				
Grade composition	Grade of exam				
Credit points (ECTS):	10	Presence study (h):	90	Self-study (h):	210
Learning outcomes:					
Extended mathematical competences regarding methods for dealing with linear structures And a deepened understanding for algebraic methods and their relationship to geometric questions. Extended capability of expressing and presenting mathematical reasoning. Competence in applying mathematical theories.					

Course overview: <ul style="list-style-type: none"> • Euclidean and unitary vector spaces • orthonormalization algorithm • orthogonal and unitary endomorphisms • quadrics • Jordan normal form • multilinear algebra
Reading list:  G. Fischer: <i>Lineare Algebra</i>
Recommended previous knowledge: <ul style="list-style-type: none"> • Algebraic methods I
if applicable entrance requirement and if applicable restriction of participants:
Applicability: <ul style="list-style-type: none"> • Bachelor programme Mathematics




Module name, Nr.	Advanced algebraic methods (Fortgeschrittene algebraische Methoden)		0103
Regularity	Wintersemester, annually		
Responsibility of module	Institut für Algebra, Zahlentheorie und Diskrete Mathematik und Institut für Algebraische Geometrie		
Course(SWS)	lecture „Algebra I“ (4 SWS) tutorial on „Algebra I“ (2 SWS)		
Major course assessment for acquisition of LP	The Course achievement is to be performed at the Tutorial Examination performance: Exam or oral examination		
Grade composition	Grade of exam or of oral examination		
Credit points (ECTS):	10	Presence study (h): 90	Self-study (h): 210
Learning outcomes: Deepening of the understanding of algebraic structures; insight into the interconnectedness of mathematical fields via applications of algebraic methods in elementary number theory and towards the solution of classical geometric construction problems. Competence for independent development of advanced mathematical reasoning related to the topics of the course, and presentation in the problem classes.			
Course overview: Arithmetic of the integers; groups (permutation groups, symmetry groups, group actions); rings (ideals, polynomial rings, divisibility, Euclidean rings, prime factorization); arithmetic modulo n (congruences, prime residue class groups); fields (algebraic field extensions, constructions with ruler and compass, cyclotomic fields, finite fields).			
Reading list:  G. Fischer: <i>Lehrbuch der Algebra</i>  E. Kunz: <i>Algebra</i>  J. Wolfart: <i>Einführung in die Zahlentheorie und Algebra</i>			
Recommended previous knowledge: <ul style="list-style-type: none"> • Algebraic methods I + II 			
if applicable entrance requirement and if applicable restriction of participants:			
Applicability: <ul style="list-style-type: none"> • Bachelor programme Mathematics 			

As module „Algebra I“ also for:

- Fächerübergreifender Bachelorstudiengang
- Masterstudiengang Lehramt Gymnasium (Zweifach)

Module name, Nr.	Praktische Verfahren der Mathematik (Praktische Verfahren der Mathematik)		0301
Regularity	Winter term and summer term, annually		
Responsibility of module	Institut für Angewandte Mathematik		
Course(SWS)	Lecture „Numerische Mathematik I“ (4 SWS) Tutorial on „Numerische Mathematik I“ (2 SWS) Lecture „Algorithmisches Programmieren“ (2SWS) Tutorial on „Algorithmisches Programmieren“ (1 SWS)		
Major course assessment for acquisition of LP	Course achievement: the tutorial on „Numerische Mathematik I“ Examination performance: written exam of „Numerische Mathematik I“ and practical programming exam of „Algorithmisches Programmieren“		
Grade composition	Weighted average of grades in written exam (weight 10) and in practical programming exam (weight 4)		
Credit points (ECTS):	14	Presence study (h):	180 Self-study (h): 240
<p>Learning outcomes:</p> <p>„Numerische Mathematik I“: Knowledge of numerical methods for approximatively solving basic mathematical problems. Assessing the suitability of different methods. Being aware of areas of application and limitations of numerical methods.</p> <p>„Algorithmic programming“: Capability of using programming languages in modeling and in solving problems from various fields of mathematics and its application areas.</p>			
<p>Course overview:</p> <p>Numerische Mathematik I: Interpolation of functions by polynomials and splines. Quadrature formulae for numerical integration. Direct methods for linear systems of equations: LU and Cholesky decomposition. Iterative methods for linear systems of equations: Jacobi, Gauss-Seidel, CG. Newton's method for systems of nonlinear equations. Condition of mathematical problems and stability of numerical algorithms.</p> <p>Algorithmic programming: Implementing and testing basic numerical algorithms in a higher programming language.</p>			
<p>Reading list:</p> <p>📖 P. Deuffhard, A. Hohmann: <i>Numerische Mathematik I</i>. De Gruyter.</p> <p>📖 A. Quarteroni, R. Sacco, F. Saleri: <i>Numerische Mathematik I und II</i>, Springer-Verlag.</p>			
<p>Recommended previous knowledge:</p> <ul style="list-style-type: none"> • Lineare Algebra I (and II) and Analysis I (and II) 			
<p>if applicable entrance requirement and if applicable restriction of participants:</p>			
<p>Applicability:</p> <ul style="list-style-type: none"> • Bachelor programme Mathematics 			

Module name, Nr.	Stochastic Methods (Stochastische Methoden)	0401
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Regularity	Summer Semester, Annually		
Responsibility of module	Institut für Mathematische Stochastik		
Course(SWS)	lecture „Mathematische Stochastik I“ (4 SWS) Tutorial „Mathematische Stochastik I“ (2 SWS)		
Major course assessment for acquisition of LP	Course achievement: Tutorial Examination performance: Exam		
Grade composition	Grade of exam		
Credit points (ECTS):	10	Presence study (h):	90 Self-study (h): 210
Learning outcomes: Basic knowledge of combinatorics, probability, and statistics. Students should understand elementary stochastic models and techniques, and be able to formulate, analyse and solve simple problems involving randomness.			
Course overview: The lecture provides an introduction to probability and statistics. Topics include: <ul style="list-style-type: none"> • Combinatorics • Axioms of probability theory • Conditional Probability and independence • Random variables and their distributions • Expectation and variance • Modes of convergence • Limit theorems for sums of independent random variables • Elementary statistics 			
Reading list:  Georgii, H.: <i>Stochastik</i> , de Gruyter  Jacod, J. & Protter. P: <i>Probability Essentials</i> , Springer  Krengel, U.: <i>Einführung in die Wahrscheinlichkeitstheorie und Statistik</i>			
Recommended previous knowledge: <ul style="list-style-type: none"> • Lineare Algebra I (and II) • Analysis I (and II) 			
if applicable entrance requirement and if applicable restriction of participants:			
Applicability: <ul style="list-style-type: none"> • Bachelor programme Mathematics • Fächerübergreifender Bachelorstudiengang (Erstfach) • Masterstudiengang Lehramt Gymnasium (Zweitfach) 			

Module name, Nr.	Proseminar	0001
Regularity	wintersemester and summersemester, annual	
Responsibility of module	Institutes of mathematics	
Course(SWS)	Proseminar (2 SWS)	
Major course assessment for acquisition of LP	Seminar performance with written composition	
Grade composition	Grade of seminar performance	

Credit points (ECTS):	5	Presence study (h):	30	Self-Study (h):	120
Learning outcomes:					
Written description of a concrete mathematical topic, its surrounding and if so its historic background. Oral presentation of results. Ability to discuss with other participants. Use of suitable media (black board, PC, projector) for preparation and presentation.					
Course overview:					
variable, depends on topic of proseminar.					
Reading list:					
variable, depends on topic of proseminar.					
Recommended previous knowledge:					
Analytic and algebraic methods					
if applicable entrance requirement and if applicable restriction of participants:					
Applicability:					
<ul style="list-style-type: none"> • Bachelor programme Mathematics 					

Compulsory elective modules Bachelor

Module name, Nr.	Basics Bachelor Algebra, number theory, discrete mathematics (Grundlagen Bachelor Algebra, Zahlentheorie, Diskrete Mathematik)		0104
Responsibility of module	Institut für Algebra, Zahlentheorie und Diskrete Mathematik und Institut für Algebraische Geometrie		
Course	lecture with tutorial (4+2): Algebra II or Discrete mathematics (see appendix) Alternative courses can be assigned to this module in the university calendar.		
Major course assessment for acquisition of LP	Course achievement: at university lecturer's option Examination performance: oral examination or Exam		
Credit points (ECTS):	10	Presence study (h): 90	Self-study (h): 210
Learning outcomes:			
Extended knowledge in an area of algebra or basic knowledge in number theory; understanding of relational and operational structures and their algebraic treatment.			
Knowledge of basic functions in combinatorics, including methods and applications. Solid grasp of mathematical argumentation and methodology. Students are able to solve concrete problems using suitable methods.			
if applicable entrance requirement and if applicable restriction of participants:			
Applicability:			
<ul style="list-style-type: none"> • Bachelor programme Mathematics 			

Module name, Nr.	Basics Bachelor Analysis (Grundlagen Bachelor Analysis)		0204
Responsibility of module	Institut für Analysis und Institut für Differentialgeometrie		
Course	lecture with tutorial (4+2): Complex analysis or Manifolds (see appendix) Alternative courses can be assigned to this module in the university calendar.		
Major course assessment for acquisition of LP	Course achievement: at university lecturer's option Examination performance: oral examination or Exam		
Credit points (ECTS):	10	Presence study (h): 90	Self-study (h): 210

Learning outcomes:

Deepened acquisition of analytic thinking based on topics in complex analysis, topology and functional analysis. Sound knowledge and reliable command of mathematical thinking and argumentation. Students gain the ability to solve concrete tasks by applying suitable methods.

if applicable entrance requirement and if applicable restriction of participants:

Applicability:

- Bachelor programme Mathematics

Module name, Nr.	Basics Bachelor Geometry (Grundlagen Bachelor Geometrie)		0501
Responsibility of module	Institut für Algebraische Geometrie und Institut für Differentialgeometrie		
Course	lecture with tutorial (4+2): Algebra II or Manifolds (see appendix) Alternative courses can be assigned to this module in the university calendar.		
Major course assessment for acquisition of LP	Course achievement: at university lecturer's option Examination performance: oral examination or Exam		
Credit points (ECTS):	10	Presence study (h):	90 Self-study (h): 210
Learning outcomes: Understanding of geometric constructions, structures in space and the interplay of algebraic, geometric, analytic, and topological methods. Sure command of mathematical reasoning. Students are able to solve explicit problems using appropriate methods.			
if applicable entrance requirement and if applicable restriction of participants:			
Applicability: <ul style="list-style-type: none"> Bachelor programme Mathematics 			

Module name, Nr.	Basics Bachelor Numerics (Grundlagen Bachelor Numerik)		0302
Responsibility of module	Institut für Angewandte Mathematik		
Course	Lecture and tutorial (4+2): Numerical Mathematics II (see appendix) Alternative courses can be assigned to this module in the university calendar.		
Major course assessment for acquisition of LP	Course achievement: at the instructor's option Examination performance: oral or written exam		
Credit points (ECTS):	10	Presence study (h):	90 Self-study (h): 210

Learning outcomes:

Knowledge of numerical methods for approximately solving demanding mathematical problems. Assessing the suitability of different methods depending on the circumstances and on the limitations of numerical methods. Proficiency in the mathematical way of thinking and arguing. Students are capable of solving concrete problems by applying suitable methods.

if applicable entrance requirement and if applicable restriction of participants:

Applicability:

- Bachelor programme Mathematics

Module name, Nr.	Basics Bachelor Stochastics (Grundlagen Bachelor Stochastik)	0402
Responsibility of module	Institut für Mathematische Stochastik	
Course	lecture with tutorial (4+2): Probability and Statistics II (see appendix) Alternative courses can be assigned for this module in university calendar.	
Major course assessment for acquisition of LP	Course achievement: at university lecturer's option Examination performance: oral examination or Exam	
Credit points (ECTS): 10	Presence study (h): 90	Self-study (h): 210
Learning outcomes: Probability, Statistics and their Applications. Students understand key mathematical concepts and arguments, and can solve exercises using appropriate methods.		
if applicable entrance requirement and if applicable restriction of participants:		
Applicability: <ul style="list-style-type: none"> • Bachelor programme Mathematics 		

Module name, Nr.	Specialisation Bachelor Algebra, number theory, discrete mathematics (Spezialisierung Bachelor Algebra, Zahlentheorie, Diskrete Mathematik)	0105
Responsibility of module	Institut für Algebra, Zahlentheorie und Diskrete Mathematik und Institut für Algebraische Geometrie	
Course	Lectures that belong to this module can be found in appendix. Further courses can be assigned for this module in the university calendar.	
Major course assessment for acquisition of LP	Course achievement: at university lecturer's option Examination performance: oral examination	

Credit points (ECTS):	10	Presence study (h):	90	Self-study (h):	210
Learning outcomes: Advanced understanding of algebraic arguments and methods, good knowledge of two areas of algebra or number theory. Advanced knowledge of the theory of relational and operational structures and their applications, for instance in coding theory, applied algebra or algebraic combinatorics. The students have a good grasp of the logical structures of the subject; they are able to derive the key results and produce the most important examples. They can analyse problems from the area and identify as well as apply methods suitable for solving them. The students are capable of explaining and justifying their approach.					
if applicable entrance requirement and if applicable restriction of participants:					
Applicability: <ul style="list-style-type: none">• Bachelor programme Mathematics					

Module name, Nr.	Specialisation Bachelor Analysis (Spezialisierung Bachelor Analysis)		0205
Responsibility of module	Institut für Analysis, Institut für Differentialgeometrie und Institut für Angewandte Mathematik		
Course	Lectures that belong to this module can be found in appendix. Further courses can be assigned for this module in the university calendar.		
Major course assessment for acquisition of LP	Course achievement: at university lecturer's option Examination performance: oral examination		
Credit points (ECTS):	10	Presence study (h):	90 Self-study (h): 210
Learning outcomes: Deepened understanding of general analytic, topological and function theoretical methods. Knowledge of qualitative methods for the investigation and solution of ordinary and partial differential equations. The students understand the logical structure of the area, they are able to deduce the most important theorems and they are aware of prominent examples. Students are capable to analyze problems of the area and to identify and apply suitable methods for their solution. They can justify and clearly explain their approach.			
if applicable entrance requirement and if applicable restriction of participants:			
Applicability: <ul style="list-style-type: none"> • Bachelor programme Mathematics 			

Module name, Nr.	Specialisation Bachelor Geometry (Spezialisierung Bachelor Geometrie)		0502
Responsibility of module	Institut für Algebraische Geometrie und Institut für Differentialgeometrie		
Course	Lectures that belong to this module can be found in appendix. Further courses can be assigned for this module in the university calendar .		
Major course assessment for acquisition of LP	Course achievement: at university lecturer's option Examination performance: oral examination		
Credit points (ECTS):	10	Presence study (h):	90 Self-study (h): 210

Learning outcomes:

In depth knowledge of the relations between algebraic, geometric, analytic and topological structures connecting geometric intuition and axiomatic foundations of the field. Students are familiar with the logical structure of the field, are able to deduce the most important statements and know illustrating examples. Students are able to analyze problems in the subject area and to identify and apply appropriate methods to tackle given problems. They know how to justify their approach and explain it clearly.

if applicable entrance requirement and if applicable restriction of participants:

Applicability:

- Bachelor programme Mathematics

Module name, Nr.	Specialisation Bachelor Numerics (Spezialisierung Bachelor Numerik)		0303
Responsibility of module	Institut für Angewandte Mathematik		
Course	Lectures in the appendix that belong to this module. Further courses can be assigned to this module in the university calendar.		
Major course assessment for acquisition of LP	Course achievement: at the instructor's option Examination performance: oral exam		
Credit points (ECTS):	10	Presence study (h):	90 Self-study (h): 210
Learning outcomes: Deepened knowledge of numerical methods for approximately solving concrete mathematical problems. Students have comprehended the logical structure of the area. They are capable of deriving the most important facts and know prominent examples. Students are capable of analyzing problems in the area and to identify and apply suitable solution methods. They can substantiate their approach and explain it comprehensively.			
if applicable entrance requirement and if applicable restriction of participants:			
Applicability: <ul style="list-style-type: none"> • Bachelor programme Mathematik 			

Module name, Nr.	Specialisation Bachelor Stochastics (Spezialisierung Bachelor Stochastik)		0403
Responsibility of module	Institut für Mathematische Stochastik		
Course	Lectures that belong to this module can be found in appendix. Further courses can be assigned for this module in the university calendar.		
Major course assessment for acquisition of LP	Course achievement: at university lecturer's option Examination performance: oral examination		
Credit points (ECTS):	10	Presence study (h):	90 Self-study (h): 210

Learning outcomes:

Extended knowledge of probability, statistics and their applications. Students understand the key concepts and methods of the field, are able to prove the main results and know important examples and applications. Students can analyse problems, can identify suitable methods for their solution and are able to apply them appropriately. They can justify their solutions strategies and explain them clearly.

if applicable entrance requirement and if applicable restriction of participants:

Applicability:

- Bachelor programme Mathematics

Module name, Nr.	Seminar		0950
Regularity	Start all year long possible		
Responsibility of module	Institutes of mathematics		
Course (SWS)	Seminar (2 SWS)		
Major course assessment for acquisition of LP	Presentation with written elaboration		
Grade composition	Grade of seminar participation		
Credit points (ECTS):	5	Presence study (h) 30	Self-study (h): 120
Learning outcomes: Ability of familiarization in a mathematical topic under guidance. Knowledge acquisition from partly English speaking books und professional journals. Academic writing skills. Presentation skills and use of media. Ability to discuss mathematical topics.			
Course overview: Introduction to academic research and writing <ul style="list-style-type: none"> • focused academic topic of mathematics after agreement with supervising tutor, • use of specialist literature/ database; • mathematic inscribing; • presentation skills and use of media; With this seminar the introduction of the bachelor thesis is getting prepared.			
Reading list: variable, depends on topics of Seminars.			
Recommended previous knowledge: variable, depends on topics of Seminars.			
In-depth specialisation for a mathematical topic as part of a seminar			
if applicable entrance requirement and if applicable restriction of participants:			
Applicability: <ul style="list-style-type: none"> • Bachelor programme Mathematik 			

Module name, Nr.	Bachelorthesis	0901
Regularity	Start all year long possible	
Responsibility of module	Institutes of mathematics	
Course(SWS)	Project „Bachelorarbeit“ (13 LP)	
Major course assessment for acquisition of LP	Examination performance: Bachelorthesis	
Grade composition	grade of Bachelorthesis	
Credit points (ECTS):	13	Presence study (h) & Self-study (h): 390
Learning outcomes:		
Ability to independently work in a research topic. Knowledge acquisition from partly english speaking books and professional journals. Ability for realistic planning, timing and for conducting an academic project with the help of academic methods under guidance. Academic writing skills. Ability to discuss own thesis and self-reflection skills.		
Course overview:		
Introduction into academic research, independent projektwork under guidance, academic writing		
<ul style="list-style-type: none"> • a focused academic topic of mathematics after agreement with supervising tutor, • use of specialist literature/Database; • mathematic inscribing; • Presentation skills and use of media; • Planning of Bachelorthesis. 		
Reading list:		
Recommended previous knowledge: Deepening of a mathematic topic in context of a seminar		
if applicable entrance requirement and if applicable restriction of participants: minimum of 120 LP		
Applicability:		
<ul style="list-style-type: none"> • Bachelor programme Mathematics 		
Examination procedure:		
The topic of the bachelor thesis will be fixed by the examiner after consultation with examination candidate. The Issuing is to be put on record and the examination candidate as well as the Studiendekanat must be informed in written form. With the Issuing of the topic the examiner will be booked. During the making of thesis the student will be looked after by the examiner.		

Modules of Master Mathematics

Module name, Nr.	Elective module 1			0004
Responsibility of module	Institutes of mathematics			
Course(SWS)	A lecture with tutorial (4V + 2Ü)			
Major course assessment for acquisition of LP	Course achievement: at university lecturer's option Examination performance: oral examination or Exam			
Grade composition	grade of oral exam or written exam			
Credit points (ECTS):	10	Presence study (h):	90	Self-study (h): 210
Learning outcomes: The students widen their mathematic knowledge. They gain an insight into a chosen field of mathematics. They acquire the skill to deal competently with problems of that particular field.				
if applicable entrance requirement and if applicable restriction of participants:				
Applicability: <ul style="list-style-type: none"> Master programme mathematics 				

Module name, Nr.	Elective module 2			0005
Responsibility of module	Institutes of mathematics			
Course(SWS)	A lecture with tutorial (4V + 2Ü)			
Major course assessment for acquisition of LP	Course achievement: at university lecturer's option Examination performance: oral examination or Exam			
Grade composition	grade of oral exam or written exam			
Credit points (ECTS):	10	Presence study (h):	90	Self-study (h): 210
Learning outcomes: The students widen their mathematic knowledge. They gain an insight into a chosen field of mathematics. They acquire the skill to deal competently with problems of that particular field.				
if applicable entrance requirement and if applicable restriction of participants:				
Applicability: <ul style="list-style-type: none"> Master programme mathematics 				

Module name, Nr.	Elective module 3			0056
Responsibility of module	Institutes of mathematics			

Course(SWS)	A lecture with tutorial (4V + 2Ü)		
Major course assessment for acquisition of LP	Course achievement: at university lecturer's option Examination performance: oral examination or Exam		
Grade composition	grade of oral exam or written exam		
Credit points (ECTS):	10	Presence study (h):	90 Self-study (h): 210
Learning outcomes:			
The students widen their mathematic knowledge. They gain an insight into a chosen field of mathematics. They acquire the skill to deal competently with problems of that particular field.			
if applicable entrance requirement and if applicable restriction of participants:			
Applicability:			
<ul style="list-style-type: none"> • Master programme mathematics 			

Module name, Nr.	Elective module 4		0057
Responsibility of module	Institutes of mathematics		
Course(SWS)	A lecture with tutorial (4V + 2Ü)		
Major course assessment for acquisition of LP	Course achievement: at university lecturer's option Examination performance: oral examination or Exam		
Grade composition	grade of oral exam or written exam		
Credit points (ECTS):	10	Presence study (h):	90 Self-study (h): 210
Learning outcomes:			
The students widen their mathematic knowledge. They gain an insight into a chosen field of mathematics. They acquire the skill to deal competently with problems of that particular field.			
if applicable entrance requirement and if applicable restriction of participants:			
Applicability:			
<ul style="list-style-type: none"> • Master programme mathematics 			

Module name, Nr.	Elective module 5		0004
Responsibility of module	Institutes of mathematics		
Course(SWS)	A lecture with tutorial (4V + 2Ü)		
Major course assessment for acquisition of LP	Course achievement: at university lecturer's option Examination performance: oral examination or Exam		

Grade composition		grade of oral exam or written exam		
Credit points (ECTS):	10	Presence study (h):	90	Self-study (h): 210
Learning outcomes:				
The students widen their mathematic knowledge. They gain an insight into a chosen field of mathematics. They acquire the skill to deal competently with problems of that particular field.				
if applicable entrance requirement and if applicable restriction of participants:				
Applicability:				
<ul style="list-style-type: none"> Master programme mathematics 				

Module name, Nr.	Elective module 6			0004
Responsibility of module	Institutes of mathematics			
Course(SWS)	A lecture with tutorial (4V + 2Ü)			
Major course assessment for acquisition of LP	Course achievement: at university lecturer's option Examination performance: oral examination or Exam			
Grade composition	grade of oral exam or written exam			
Credit points (ECTS):	10	Presence study (h):	90	Self-study (h): 210
Learning outcomes:				
The students widen their mathematic knowledge. They gain an insight into a chosen field of mathematics. They acquire the skill to deal competently with problems of that particular field.				
if applicable entrance requirement and if applicable restriction of participants:				
Applicability:				
<ul style="list-style-type: none"> Master programme mathematics 				

Module name, Nr.	Key Skills (Schlüsselkompetenzen)		0060
Semesterlage	every semester		
Responsibility of module	Institutes of mathematics		
Course(SWS)	two seminars (each 2 SWS)		
Major course assessment for acquisition of LP	Examination performance: Seminar performance in every seminar		
Grade composition	Overall average grade of both seminar performances		
Credit points (ECTS):	10	Presence study (h): 60	Self-study (h): 240
Learning outcomes: The students have the ability to independently work in a research topic. This contains especially the independent research of specialist literature for a given topic and the knowledge acquisition from specialised books and articles. Students can recognize connections in regard to content. They acquire knowledge of the English language to be able to study relevant specialist literature. The students are in the position to structure a complex topic of the modern mathematic in a suitable way and to understandable recite. They are capable of having an academic discussion and of self-reflecting.			
Course overview: Depends on lecture. Current topics of different mathematic fields.			
if applicable entrance requirement and if applicable restriction of participants:			
Applicability: <ul style="list-style-type: none"> Master programme mathematics 			

Module name, Nr.	Masterthesis (Masterarbeit)	0902
Semesterlage	Start all year long possible	
Responsibility of module	Institutes of mathematics	
Course(SWS)	Projekt „Masterarbeit“	
Major course assessment for acquisition of LP	Course achievement: Presentation Examination performance: Masterthesis	
Grade composition	Grade of master thesis (Overall average grade of the two examiner opinions)	
Credit points (ECTS):	30	Arbeitsaufwand(h): 900
Learning outcomes:		
<p>The students can independently work in a research. They are able to structure, to prepare and to undertake scientific projects under guidance. They procure an overview over the recent literature and they analyse and solve complex problems. The students can hold critical discussions about their own and external research results and interact constructive with questions and critics. They have the competence to pose self-dependent mathematical facts.</p>		
Course overview:		
Introduction into academic research, independent projektwork under guidance, academic writing.		
<ul style="list-style-type: none"> • a current academic topic of mathematics after agreement with supervising tutor, • mathematic inscribing; • current specialist literature/Database . 		
if applicable entrance requirement and if applicable restriction of participants: minimum 75 LP, Completion of the module key skills		
Applicability:		
<ul style="list-style-type: none"> • Master programme mathematics 		
Examination procedure:		
<p>The topic of the master thesis will be fixed by the first examiner after consultation with examination candidate. The Issuing is to be put on record and the examination candidate as well as the Studiendekanat must be informed in written form. With the Issuing of the topic the first examiner and second examiner will be booked. During the making of thesis the student will be looked after by the first examiner.</p>		

Appendix:

Below lectures will be described that can be taken for compulsory elective modules of the Bachelorstudy and for Mastermodules .

The Lectures in **Appendix A** can be taken for the Basics modules Bachelor and in parts for the Specialization modules Bachelor. The lectures in **Appendix B** can be taken for the Mastermodules and in parts for the Specialization modules Bachelor.

The letters **R** and **A** in the upper right-hand corner of the lecture descriptions define the assignment of the lecture to the Abstract (German: Reinen) mathematics or applied (German: Angewandten) mathematics.

Those ******* seen at the Semesterweekhours (Short: **SWS**, in german: Semesterwochenstundenzahl) and credit points mean that the course is offered depending on overall supply of that particular Semester as lecture with 4+2 SWS/ 10 CP or with 2+1 SWS/ 5 CP or if applicable as seminar . More detailed information can be found in the university calendar

Those used abbreviation mean:

[IAG „Institut für Algebraische Geometrie“;](#)

[IAZD „Institut für Algebra, Zahlentheorie und Diskrete Mathematik“,](#)

[IDG „Institut für Differentialgeometrie“](#)

[IFAM „Institut für Angewandte Mathematik“;](#)

[IFMS „Institut für Mathematische Stochastik“.](#)


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A. Lectures for basics modules Bachelor

Algebra II			R
Type of course Bachelor	SWS 4+2	Credit points: 10	Responsibility IAZD and IAG
Regularity: annual, summersemester			
Course overview: <ul style="list-style-type: none"> • Field theory (structure of finitely generated field extensions), Galois theory, solvability of algebraic equations • Modules and algebras (Noetherian rings, Hilbert's Basis Theorem, integral ring extensions, modules over principal ideal rings, Artin-Wedderburn Theorem, tensor products) 			
Reading list:  J.C. Jantzen, J. Schwermer: <i>Algebra</i> , Springer 2006			
Recommended previous knowledge: Algebra I			
Module affiliation: <ul style="list-style-type: none"> • Basics Bachelor Algebra, Number theory, Discrete mathematics • Basics Bachelor Geometry • Specialization Bachelor Algebra, Number theory, Discrete mathematics • Specialization Bachelor Geometry 			

Discrete Mathematics (Diskrete Mathematik)			R
Type of course Bachelor	SWS 4+2	Credit points: 10	Responsibility IAZD
Regularity: annual, summersemester			

Course overview:

- Enumerations and Combinatorics
- Generating functions
- Theory of graphs
- Error-correcting codes
- Algebraic combinatorics or oriented matroids

Reading list:

- 📖 M. Aigner: *Diskrete Mathematik*
- 📖 Harary: *Graphentheorie*
- 📖 A. Björner et al.: *Oriented Matroids*

Recommended previous knowledge: Algebra I



Module affiliation:

- Basics Bachelor Algebra, Number theory, Discrete mathematics

Mannigfaltigkeiten			R
Art der Vorlesung Bachelor	SWS 4+2	Credit points: 10	Verantwortung IDG
Regelmäßigkeit: annually, Sommersemester			
Inhalt: <ul style="list-style-type: none"> • Topologische und differenzierbare Manigfaltigkeiten • Tangential- und Kotangentialräume und - bündel • Differentialformen und Vektorfelder • Lie-Ableitungen, Lie-Gruppen und -Algebren • Integration auf Mannigfaltigkeiten, der Satz von Stokes • Vektorbündel und Tensorfelder • Zusammenhänge auf Vektorbündeln, Paralleltransport, kovariante Ableitung und Holonomie 			
Grundlegende Literatur: <ul style="list-style-type: none"> 📖 Boothby, William M., <i>An introduction to differentiable manifolds and Riemannian geometry</i>, Academic Press, Inc., Orlando, FL, 1986 📖 Milnor: <i>Topology from the Differentiable Viewpoint</i>, Princeton University Press 📖 Lee, John M., <i>Introduction to smooth manifolds</i>, Graduate Texts in Mathematics 218, Springer-Verlag, New York 📖 Warner, Frank W., <i>Foundations of differentiable manifolds and Lie groups</i>, Graduate Texts in Mathematics 94, Springer-Verlag New York-Berlin 			
Empfohlene Vorkenntnisse: Analysis III			
Module affiliation: <ul style="list-style-type: none"> • Basics Bachelor Analysis • Basics Bachelor Geometry • Specialization Bachelor Analysis • Specialization Bachelor Geometry • elective module Master Mathematik 			

Complex Analysis (Funktionentheorie)			R
Type of course Bachelor	SWS 4+2	Credit points: 10	Responsibility Institute for Analysis
Regularity: annual, sommersemester			
Course overview: <ul style="list-style-type: none"> • Holomorphic und meromorphic functions • Cauchy's integral theorem • Local mapping properties of holomorphic functions • Residue theorem • Riemann mapping theorem 			
Reading list: <ul style="list-style-type: none"> • L. Ahlfors: <i>Complex Analysis</i>, McGraw-Hill, New York, 1978. • J. Conway: <i>Functions of one Complex Variable</i>, Springer-Verlag, New York 1995. 			




<ul style="list-style-type: none"> W. Rudin: <i>Real and Complex Analysis</i>, McGraw-Hill, New York, 1987.
Recommended previous knowledge: Analysis I-III
Module affiliation: <ul style="list-style-type: none"> Basics Bachelor Analysis Specialization Bachelor Analysis


Numerical Mathematics II (Numerische Mathematik II)			A
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility IFAM
Regularity: annually, summer term			
Course overview: Numerical methods for eigenvalue problems: inverse Iteration, QR algorithm, Lanczos method. Initial value problems for ordinary differential equations: Runge-Kutta methods, adaptive stepsize control, stiff differential equations.			
Reading list:  P. Deuflhard, V. Bornemann: <i>Scientific Computing with Ordinary Differential Equations</i> , Springer-Verlag.  A. Quarteroni, R. Sacco, F. Saleri: <i>Numerische Mathematik I and II</i> , Springer-Verlag.			
Recommended previous knowledge: Numerical Mathematics I			
Module affiliation: <ul style="list-style-type: none"> Basics Bachelor Numerics Specialization Bachelor Numerics For an in-depth module it can be combined with: <ul style="list-style-type: none"> all lectures for applied mathematics or alternative lectures in agreement with examiner			



Probability and Statistics II (Mathematische Stochastik II)			A
Type of course Bachelor	SWS 4+2	Credit points: 10	Responsibility IFMS
Regularity: annually, Wintersemester			
<p>Course overview:</p> <ul style="list-style-type: none"> • Measure Thoery • Limit Theorems • Martingales • Statistics: Estimators, Confidence Sets, Statistical Tests <p>Reading list:</p> <ul style="list-style-type: none"> • P. Billingsley: <i>Probability and Measure</i>, Wiley, New York, 1995. • L. Rüschendorf: <i>Mathematische Statistik</i>, Springer, Berlin, 2014. • Georgii, H.: <i>Stochastik</i>, de Gruyter • Jacod, J. & Protter. P: <i>Probability Essentials</i>, Springer <p>Recommended previous knowledge: Probability and Statistics I</p>			
<p>Module affiliation:</p> <ul style="list-style-type: none"> • Basics Bachelor Stochastics • Specialization Bachelor Stochastics 			

B. Lectures for master modules



B.1 Algebra, Number theory and Discrete mathematics:




Algebraic Combinatorics (Algebraische Kombinatorik)			R
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility IAZD
Regularity: irregular			
<p>Course overview: In Algebraic Combinatorics, on the one hand methods from algebra, in particular group theory and representation theory, are applied towards combinatorial problems, on the other hand, combinatorial approaches are fruitfully employed in algebraic contexts. Topics in this area of interaction are in particular concerned with:</p> <ul style="list-style-type: none"> • Young tableaux and partitions • symmetric functions • weighted enumeration under group actions • symmetric groups <p>Reading list:  W. Fulton: <i>Young Tableaux</i>  R. Stanley: <i>Enumerative Combinatorics II</i>  R. Stanley: <i>Algebraic Combinatorics</i></p>			
Recommended previous knowledge: Algebra I, Basics of combinatorics			
<p>Module affiliation:</p> <ul style="list-style-type: none"> • Specialization Bachelor Algebra, Number theory, Discrete mathematics • Elective Modules of Master Mathematics <p>For an in-depth module it can be combined with e.g.: Enumerative combinatorics, Representation theory</p>			

Algebraic Number Theory I (Algebraische Zahlentheorie I)			R
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility IAZD
Regularity: every two years, wintersemester			
<p>Course overview: Introduction to algebraic number theory, detailed treatment of the following topics:</p> <ul style="list-style-type: none"> • arithmetic of algebraic number fields • zeta- and L-series <p>Reading list:</p> <p> Neukirch: <i>Algebraische Zahlentheorie</i></p> <p>Recommended previous knowledge: Algebra II</p>			
<p>Module affiliation:</p> <ul style="list-style-type: none"> • Specialization Bachelor Algebra, Number theory, Discrete mathematics • Elective module master Mathematics 			





Algebraic Number Theory II (Algebraische Zahlentheorie II)			R
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility IAZD
Regularity: every 2 years, summersemester			
<p>Course overview: Advanced treatment of algebraic number theory via one or more of the following topics:</p> <ul style="list-style-type: none"> • p-adic number fields • class field theory • algorithmic problems <p>Reading list:</p> <p> Neukirch: <i>Algebraische Zahlentheorie</i></p> <p> Cohen: <i>Topics in Computational Algebraic Number Theory</i></p> <p>Recommended previous knowledge: Algebraic Number Theory I</p>			
<p>Module affiliation:</p> <ul style="list-style-type: none"> • Specialization Bachelor Algebra, Number theory, Discrete mathematics • Elective module master Mathematics 			

Algebras and their representations (Algebren und ihre Darstellungen)			R
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility IAZD
Regularity: irregular			

<p>Course overview: An example-driven introduction to the representation theory of finite-dimensional algebras and to representations of quivers. Topics covered include:</p> <p>Representations of finite-dimensional algebras: indecomposable modules and the Krull-Schmidt theorem; representation type; projective and injective modules; introduction to the language of categories and functors; Ext-functors.</p> <p>Representations of quivers: hereditary algebras; quadratic forms associated to quivers; reflection functors; Gabriel's theorem on the representation type of quivers; Dynkin diagrams.</p> <p>Reading list:</p> <ul style="list-style-type: none">  K. Erdmann, T. Holm: <i>Algebras and Representation Theory</i> (Manuskript kann zur Verfügung gestellt werden).  Assem, D. Simson, A. Skowronski: <i>Elements of the Representation theory of Associative Algebras 1: Techniques of Representation Theory</i>, London Mathematical Society Student Texts 65, Cambridge University Press, 2006. <p>Recommended previous knowledge: (Einführung in die) Darstellungstheorie (A first course on representation theory.)</p>
<p>Module affiliation:</p> <ul style="list-style-type: none"> • Specialization Bachelor Algebra, Number theory, Discrete mathematics • Elective module master Mathematics

Analytic Number Theory I (Analytische Zahlentheorie I)			R
Type of course Bachelor and Master	SWS 2+2	Credit points: 5	Responsibility IAZD
Regularity: every two years, wintersemester			
<p>Course overview:</p> <p>Introduction to analytic number theory, in particular: Arithmetic functions, Dirichlet series, Perron's formula, analytic properties of the zeta function, prime number theorem, introduction to sieve methods</p> <p>Reading list:</p> <ul style="list-style-type: none">  J. Brüdern, Einführung in die analytische Zahlentheorie, Springer-Verlag, 1995.  H. Davenport, Multiplicative Number Theory, Springer-Verlag, 2000.  H.L. Montgomery and R.C.Vaughan, Multiplicative Number Theory, I. Classical Theory, Cambridge University Press, 2007. 			

Recommended previous knowledge: Complex Analysis
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Algebra, Number theory, Discrete mathematics • Elective module master Mathematics <p>In each case it can be combined with lectures of Algebra, Number theory, Discrete mathematics (in particular: Analytic Number theory II) or Analysis or alternative lectures in agreement with examiner.</p>

Analytic Number Theory II (Analytische Zahlentheorie II)			R
Type of course	SWS	Credit points:	Responsibility
Bachelor and Master	2+2	5	IAZD
Regularity: every 2 years, summersemester			
Course overview: <p>Advanced treatment of analytic number theory. Possible topics include the the Bombieri-Vinogradov theorem, Tauberian theorems, mean values and distributions of additive and multiplicative functions, applications of the Selberg-Delange and of the saddle point method.</p>			
Reading list: <ul style="list-style-type: none">  J. Brüdern, Einführung in die analytische Zahlentheorie, Springer-Verlag, 1995.  H. Davenport, Multiplicative Number Theory, Springer-Verlag, 2000.  H.L. Montgomery and R.C.Vaughan, Multiplicative Number Theory, I. Classical Theory, Cambridge University Press, 2007.  G. Tenenbaum, Introduction to analytic and probabilistic number theory, Cambridge University Press, 1995. 			
Recommended previous knowledge: Complex Analysis, Analytic Number Theory I			
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Algebra, Number theory, Discrete mathematics • Elective module master Mathematics <p>In each case it can be combined with lectures of Algebra, Number theory, Discrete mathematics (in particular: Analytic Number theory I) or Analysis or alternative lectures in agreement with examiner</p>			

Arithmetic Geometry I (Arithmetische Geometrie I)				R
Type of course	SWS	Credit points:	Responsibility	
Bachelor and Master	4+2	10	IAZD	
Regularity: every 2 years, wintersemester				
Course overview: Introductory course in arithmetic geometry, based on one of the following topics: <ul style="list-style-type: none"> • curves over finite fields • elliptic curves 				
Reading list: 📖 Lorenzini: <i>An Invitation to Arithmetic Geometry</i> 📖 Silverman: <i>The Arithmetic of Elliptic Curves</i>				
Recommended previous knowledge: Algebra II				
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Algebra, Number theory, Discrete mathematics • Elective module master Mathematics 				

Arithmetic Geometry II (Arithmetische Geometrie II)				R
Type of course	SWS	Credit points:	Responsibility	
Master	4+2	10	IAZD	
Regularity: every zwei years, summersemester				
Course overview: Advanced course on one of the following topics: <ul style="list-style-type: none"> • modular forms and modularity • diophantine geometry • arithmetic fundamental groups 				
Reading list: 📖 Diamond, Shurman: <i>A first course in modular forms</i> 📖 Hindry, Silverman: <i>Diophantine Geometry</i>				
Recommended previous knowledge: Arithmetic Geometry I or Algebraic Geometry				
Module affiliation: <ul style="list-style-type: none"> • Elective module master Mathematics 				

Representation theory (Darstellungstheorie)				R
Type of course	SWS	Credit points:	Responsibility	
Bachelor und Master	4+2	10	IAZD	

Regularity: every 2 years, wintersemester
<p>Course overview: The course provides an introduction into the theory of semisimple (associative) algebras, with a focus on group algebras and characters. Central topics are</p> <ul style="list-style-type: none"> • Modules and representations of groups and algebras (simple and semisimple modules, composition series, indecomposable modules, semisimple algebras, Jacobson radical, Artin-Wedderburn decomposition, Maschke's Theorem) • Fundamentals of the character theory of finite groups (irreducible characters, inner product for characters, orthogonality relations, computation of character tables, tensor products and products of characters) <p>Reading list:</p> <ul style="list-style-type: none"> 📖 G. James, M. Liebeck: <i>Representations and Characters of Groups</i>, Cambridge University Press, 2001 (2nd Edition). 📖 J. Jantzen, J. Schwermer: <i>Algebra</i> <p>Recommended previous knowledge: Algebra I is necessary, Algebra II is desirable</p>
<p>Module affiliation:</p> <ul style="list-style-type: none"> • Specialization Bachelor Algebra, Number theory, Discrete mathematics • Elective module master Mathematics

Representation theory of finite-dimensional algebras (Darstellungstheorie endlich-dimensionaler Algebren)			R
Type of course Master	SWS 4+2	Credit points: 10	Responsibility IAZD
Regularity: irregular			



<p>Course overview:</p> <ul style="list-style-type: none"> • Quivers with relations • Morita equivalence • Auslander-Reiten Reiten theory (irreducible morphisms, almost split sequences, Auslander-Reiten quivers) • tilting theory (torsion pairs, tilting modules, Brenner-Butler theorem) <p>Reading list:</p> <ul style="list-style-type: none"> 📖 Assem, D. Simson, A. Skowronski: <i>Elements of the Representation theory of Associative Algebras 1: Techniques of Representation Theory</i>, London Mathematical Society Student Texts 65, Cambridge University Press, 2006. 📖 M. Auslander, I. Reiten, S. Smalø: <i>Representation Theory of Artin Algebras</i>, Cambridge studies in advanced mathematics 36, Cambridge University Press, 1995. <p>Recommended previous knowledge: Algebras and their representations</p>
<p>Module affiliation:</p> <ul style="list-style-type: none"> • Elective module master Mathematics



Representation theory of symmetric groups (Darstellungstheorie symmetrischer Gruppen)			R
Type of course	SWS	Credit points:	Responsibility
Bachelor and Master	4+2	10	IAZD
Regularity: every 2 years, wintersemester			
<p>Course overview:</p> <p>Topics both from ordinary and modular representation theory of symmetric groups are covered, in particular:</p> <ul style="list-style-type: none"> • classification and properties of the irreducible characters of the symmetric groups • symmetric functions • permutation modules and Specht modules • representations in positive characteristic: simple modules and the decomposition of Specht modules <p>Reading list:</p> <ul style="list-style-type: none"> 📖 G. James, A. Kerber: <i>The Representation Theory of the Symmetric Group</i> 📖 B. Sagan: <i>The Symmetric Group</i> 📖 R. Stanley: <i>Enumerative Combinatorics II</i> 			

<p>Recommended previous knowledge: Representation theory is necessary, Groups and their representations is desirable</p>
<p>Module affiliation:</p> <ul style="list-style-type: none"> • Specialization Bachelor Algebra, Number theory, Discrete mathematics • Elective module master Mathematics

Enumerative combinatorics (Enumerative Kombinatorik)			R
Type of course Bachelor	SWS 4+2	Credit points: 10	Responsibility IAZD
Regularity: irregular			
<p>Course overview:</p> <ul style="list-style-type: none"> • generating functions for weighted combinatorial objects • bijective combinatorics • constructive combinatorics <p>Reading list:</p> <ul style="list-style-type: none"> 📖 R. Stanley: <i>Enumerative Combinatorics I, II</i> 📖 D. Stanton, D. White: <i>Constructive Combinatorics</i> <p>Recommended previous knowledge: Algebra I</p>			
<p>Module affiliation:</p> <ul style="list-style-type: none"> • Specialization Bachelor Algebra, Number theory, Discrete mathematics 			

Groups and their representations (Gruppen und ihre Darstellungen)			R
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility IAZD
Regularity: every 2 years, summersemester			
<p>Course overview: Structure of finite groups and their ordinary and modular representations; in particular, the topics are:</p> <ul style="list-style-type: none"> • continuation of the theory of complex characters: induced characters, Frobenius reciprocity, Mackey's Theorem, character degrees and character values • structure of groups: Sylow's theorems, solvable groups, Burnside's $p^a q^b$ Theorem • modular representation theory: indecomposable representations, projective and simple modules, induced representations, decomposition numbers, blocks of representations <p>Reading list:</p> <ul style="list-style-type: none"> 📖 G. James, M. Liebeck: <i>Representations and Characters of Groups</i> 📖 H. Nagao, Y. Tsushima: <i>Representations of finite groups</i> <p>Recommended previous knowledge: Algebra II, Representation theory</p>			
<p>Module affiliation:</p> <ul style="list-style-type: none"> • Specialization Bachelor Algebra, Number theory, Discrete mathematics • Elective module master Mathematics 			

Homological Algebra (Homologische Algebra)			R
Type of course Master	SWS 4+2	Credit points: 10	Responsibility IAZD
Regularity: irregular			
Course overview: Exact sequences; groups of homomorphisms; tensor products of modules over rings; projective, injective and flat modules; categories and functors; chain complexes and cochain complexes; homology and cohomology of complexes; projective and injective resolutions; derived functors; Ext-functors; Tor-functors and applications.			
Reading list:  Rotman: <i>An Introduction to Homological Algebra</i> (Second Edition)  Weibel: <i>An introduction to homological algebra</i>			
Recommended previous knowledge: Algebra II			
Module affiliation: <ul style="list-style-type: none"> Elective module master Mathematics 			

Cryptography			R/A
Art der Vorlesung Bachelor	SWS 4+2	Credit points: 10	Verantwortung IAZD/IAG
Regelmäßigkeit: unregelmäßig			
Inhalt: <ul style="list-style-type: none"> allgemeine Konzepte der Kryptographie RSA-Verfahren der diskrete Logarithmus 			
Grundlegende Literatur:  Buchmann: <i>Einführung in die Kryptographie</i>  Karpfinger, Kiechle: <i>Kryptologie, Vieweg+Teubner 2010</i>			
Empfohlene Vorkenntnisse: Algebra I			
Module affiliation: <ul style="list-style-type: none"> Spezialisierung Bachelor Algebra, Zahlentheorie, Diskrete Mathematik 			

Topology (Topologie)			R
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility IAZD
Regularity: irregular			

Course overview:

- Topological spaces, continuous maps
- connected spaces, separation axioms
- compactness
- constructions (products, quotients)
- homotopy of maps
- fundamental groups
- coverings

Reading list:


- 📖 K. Jänich: Topologie
- 📖 G. Laures, M. Szymik: Grundkurs Topologie
- 📖 B.v. Querenburg: Mengentheoretische Topologie
- 📖 R. Stöcker, H. Zieschang: Algebraische Topologie

Recommended previous knowledge: Analysis I and II

Module affiliation:

- Specialization Bachelor Algebra, Number theory, Discrete mathematics

B.2 Algebraic Geometry

Algebraic Surfaces (Algebraische Flächen)			R
Type of course Master and GRK	SWS ***	Credit points: ***	Responsibility IAG
Regularity: every 2 to 3 years, summersemester			
Course overview: <ul style="list-style-type: none"> • birational maps between surfaces • intersection theory • Kodaira classification 			
Reading list:  Beauville: <i>Complex algebraic surfaces</i> , CUP, 1983.			
Recommended previous knowledge: Algebraic Geometry, helpful: Algebra II			
Module affiliation: <ul style="list-style-type: none"> • Elective module master Mathematics 			

Algebraic Geometry I (Algebraische Geometrie I)			R
Type of course Bachelor, Master and GRK	SWS 4+2	Credit points: 10	Responsibility IAG
Regularity: annual, wintersemester			
Course overview: <ul style="list-style-type: none"> • affine and projective varieties • morphisms and rational maps • dimension, degree, smoothness, singularities • sheaves and schemes 			
Recommended previous knowledge: Algebra I; helpful: Algebra II, Complex analysis			
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Geometry • Elective module master Mathematics 			

Algebraic Geometry II (Algebraische Geometrie II)			R
Type of course	SWS	Credit points:	Responsibility
Bachelor, Master and GRK	4+2	10	IAG
Regularity: annual, summersemester			
Course overview: Some topics of Algebraic Geometry are covered in detail. Possible topics include: <ul style="list-style-type: none"> • Theory of curves • Schemes • Hilbert polynomial • Sheaf cohomology • Intersection theory • divisors 			
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Geometry • Elective module master Mathematics 			

Algebraic topology (Algebraische Topologie)			R
Type of course	SWS	Credit points:	Responsibility
Bachelor and Master	4+2	10	IAG
Regularity: irregular			
Course overview: <ul style="list-style-type: none"> • homology theory, singular homology, cell complex • cohomology theory • Poincaré duality 			
Recommended previous knowledge: Algebra I, helpful: Algebra II			
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Geometry • Specialization Bachelor Algebra, Number theory, Discrete mathematics • Elective module master Mathematics 			


Algorithmic Commutative Algebra (Algorithmische Kommutative Algebra)			R
Type of course	SWS	Credit points:	Responsibility
Bachelor and Master	4+2	10	IAG
Regularity: irregular			

Course overview: <ul style="list-style-type: none"> • Polynomial systems • Groebner Bases, syzygies, free resolutions • Dimension, integral closure, primary decomposition
Recommended previous knowledge: Algebra I; helpful: Algebra II
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Algebra, Number theory, Discrete mathematics • Specialization Bachelor Geometry • Elective module master Mathematics

Coding theory (Codierungstheorie)			R
Type of course	SWS	Credit points:	Responsibility
Bachelor and Master	4+2 (2+1)	10 (5)	IAG
Regularity: irregular			
Course overview: <ul style="list-style-type: none"> • linear codes • special good codes • decoding • cyclic codes 			
Recommended previous knowledge: Algebra I			
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Algebra, Number theory, Discrete mathematics • Specialization Bachelor Geometry • Elective module master Mathematics 			

Differential topology (Differentialtopologie)			R
Type of course Master and GRK	SWS 4+2	Credit points: 10	Responsibility: IAG
Regularity: irregular			
Course overview: <ul style="list-style-type: none"> • Differentiable manifolds and maps • tangent bundles, vector fields • dynamical systems • morse theory 			
Recommended previous knowledge: Analysis III			
Module affiliation: <ul style="list-style-type: none"> • Elective module master Mathematics 			

Plane Algebraic Curves (Ebene Algebraische Kurven)			R
Type of course Bachelor and Master, also Teaching profession	SWS 2+1	Credit points: 5	Responsibility IAG
Regularity: irregular			
Course overview: <ul style="list-style-type: none"> • Intersection of plane curves, Bezout theorem • Tangents, points of inflection, smoothness and singularities • Polar curve, Hesse curve, dual curve, Plücker formulae 			
Recommended previous knowledge: Algebra I			
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Geometry • Elective module master Mathematics 			

Lattices and Codes (Gitter und Codes)			R
Type of course	SWS	Credit points:	Responsibility
Bachelor and Master	4+2	10	IAG
Regularity: irregular			
Course overview: <ul style="list-style-type: none"> • Integral lattices • Linear codes • Weight enumerators and theta functions 			
Reading list:  W.Ebeling: <i>Lattices and Codes</i> , 3. Auflage, Springer, 2013.			
Recommended previous knowledge: Algebra I, Complex analysis			
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Geometry • Specialization Bachelor Algebra, Number theory, Discrete mathematics • Elective module master Mathematics 			

Moduli Spaces (Modulräume)			R
Type of course	SWS	Credit points:	Responsibility
Master and GRK	***	***	IAG
Regularity: every 2-3 years, summersemester			
Course overview: <ul style="list-style-type: none"> • Moduli problems, coarse and fine moduli spaces • Construction of moduli spaces, geometric invariant theory • Examples of moduli spaces, in particular moduli of curves 			
Recommended previous knowledge: Algebra II, Algebraic Geometry			
Module affiliation: <ul style="list-style-type: none"> • Elective module master Mathematics 			

Singularity			R
Type of course Master and GRK	SWS 4+2	Credit points: 10	Responsibility IAG
Regularity: irregular			
<p>Course overview:</p> <ul style="list-style-type: none"> • Holomorphic functions of several variables • Analytic set germs • Unfoldings and deformations • Classification of singularities <p>Reading list:</p> <p>📖 W. Ebeling: <i>Funktionentheorie, Differentialtopologie und Singularitäten</i>, Vieweg, 2001.</p> <p>Recommended previous knowledge: Algebra II</p>			
<p>Module affiliation:</p> <ul style="list-style-type: none"> • Elective module master Mathematics 			

B.3 Analysis

Functional Analysis (Funktionalanalysis)			R/A
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility Bauer, Escher, Schrohe, Walker
Regularity: annual			
Course overview: <ul style="list-style-type: none"> • Baire's theorem • Hahn-Banach theorem, convexity • Principle of uniform boundedness • Open mapping theorem, closed graph theorem • Linear operators in Hilbert space • Compact operators • Unbounded operators 			
Recommended previous knowledge: Analysis I-III, Linear Algebra I			
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Analysis 			

Index theory (Indextheorie)			R
Type of course Bachelor and Master	SWS 2+1	Credit points: 5	Responsibility Schrohe
Regularity: irregular			
Course overview: <ul style="list-style-type: none"> • Fredholm operators in Banach spaces • Spectral theory of compact operators and the Fredholm alternative • Components of the Fredholm operators in Hilbert spaces • Toeplitz operators and their index • Computation of the index via the operator trace • Pseudodifferential operators • Fedosov's index formula 			
Recommended previous knowledge: Analysis I-III, Linear Algebra I, Functional Analysis			
Module affiliation: Specialization Bachelor Analysis			

Pseudodifferential Operators (Pseudodifferentialoperatoren)			R/A
Type of course Bachelor and Master	SWS 2+1	Credit points: 5	Responsibility Bauer, Escher, Schrohe, Walker
Regularity: irregular			

Course overview:

- Fourier transform
- Tempered distributions
- Sobolev spaces
- Oscillatory integrals
- Symbol classes
- Continuity properties and calculus
- Ellipticity and parametrix construction
- Operators on manifolds
- Wave front sets

Recommended previous knowledge: Analysis I-III, Lineare Algebra I, Functional Analysis

Module affiliation:

- Specialization Bachelor Analysis

B.4 Angewandte Analysis

Semigroups and Evolution Equations (Halbgruppen und Evolutionsgleichungen)			R/A
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility Escher, Walker
Regularity: every one to two years			
Course overview: <ul style="list-style-type: none"> • closed operators in Banach spaces • strongly continuous and analytic semigroups • generators of semigroups • characterization theorems • semilinear Cauchy problems • fractional powers of operators • maximal regularity 			
Recommended previous knowledge: Analysis I-III, Linear Algebra I and II			
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Analysis • Elective module master Mathematics 			

Interpolation Theory and Applications (Interpolationstheorie und Anwendungen)			R/A
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility Escher, Walker
Regularity: irregular			

<p>Course overview:</p> <ul style="list-style-type: none"> • real and complex interpolation method • reiteration and duality theorems • interpolation of Lebesgue and Sobolev spaces • fractional powers of operators • interpolation theory for elliptic boundary value problems • applications to semigroup theory <p>Recommended previous knowledge: Semigroups and Evolution Equations or Functional Analysis</p>
<p>Module affiliation:</p> <ul style="list-style-type: none"> • Specialization Bachelor Analysis • Elective module master Mathematics

Nonlinear Functional Analysis (Nichtlineare Funktionalanalysis)			R/A
Type of course	SWS	Credit points:	Responsibility
Bachelor and Master	4+2	10	Escher, Walker
Regularity: every one to two years			
<p>Course overview:</p> <ul style="list-style-type: none"> • implicit function theorem in Banach spaces • degree theory • bifurcation theory <p>Recommended previous knowledge: Analysis I-III, Lineare Algebra I and II</p>			
<p>Module affiliation:</p> <ul style="list-style-type: none"> • Specialization Bachelor Analysis • Elective module master Mathematics 			

Partial Differential Equations (Partielle Differentialgleichungen)			R/A
Type of course	SWS	Credit points:	Responsibility
Bachelor and Master	4+2	10	Bauer, Escher, Schrohe, Walker
Regularity: annual			
<p>Course overview:</p> <ul style="list-style-type: none"> • method of characteristics • distribution theory • Laplace's equation, maximum principles • Sobolev spaces • variational methods • Fourier transform • wave equation • heat equation 			

Recommended previous knowledge: Analysis I-III, Linear Algebra I and II

Module affiliation:


- Specialization Bachelor Analysis
- Elective module master Mathematics

Nonlinear Partial Differential Equations (Nichtlineare partielle Differentialgleichungen)			R/A
Type of course	SWS	Credit points:	Responsibility
Master	4+2	10	Escher, Walker
Regularity: irregular			
<p>Course overview:</p> <ul style="list-style-type: none"> • nonlinear elliptic and parabolic equations • fixed point methods • variational methods • compactness methods • monotone operators 			
Recommended previous knowledge: Partial Differential Equations I			
<p>Module affiliation:</p> <ul style="list-style-type: none"> • Specialization Bachelor Analysis • Elective module master Mathematics 			


Partial Differential Equations II (Partielle Differentialgleichungen II)			A
Type of course	SWS	Credit points:	Responsibility
Master	4+2	10	Escher, Walker
Regularity: irregular			
<p>Course overview:</p> <ul style="list-style-type: none"> • Schauder-theory of elliptic boundary value problems • superlinear elliptic and parabolic equations • Fixed point methods in ordered Banach spaces • Mathematical fluid dynamics 			
Recommended previous knowledge: Partiell Differential Equations I			


Qualitative Theory of Ordinary Differential Equations (Qualitative Theorie gewöhnlicher Differentialgleichungen)			R/A
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility Escher,Walker
Regularity: annual			
Course overview: <ul style="list-style-type: none"> • dynamical systems • invariant sets • limit sets • stability and linearization principles • periodic solutions 			
Recommended previous knowledge: Analysis I-III, Linear Algebra I and II			
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Analysis • Elective module master Mathematics 			


B.5 Numerical Mathematics und Optimierung

hp-Finite Element Methods (hp-Finite Element Methoden)			A
Type of course	SWS	Credit points:	Responsibility
Bachelor and Master	2+1	5	IFAM
Regularity: regularly every 1–2 years			
Course overview: <ul style="list-style-type: none"> • Error reduction by mesh refinement and increasing degree of polynomial • Proof of exponential convergence in FEM • Proof of exponential convergence in Gauß quadrature • Application to mechanics and electrodynamics • Adaptive methods • New developments in numerical analysis 			
Reading list:  Standard literature, lecture notes			
Recommended previous knowledge: Numerical Mathematics I			
Module affiliation: Specialization Bachelor Numerics			


Linear optimization (Lineare Optimierung)			A
Type of course	SWS	Credit points:	Responsibility
Bachelor and Master	2+1	5	Steinbach
Regularity: regularly every 2–3 years			


Course overview: <ul style="list-style-type: none"> • Simplex method • Theory of polyhedra • Farkas lemma and extensions • Duality theory
Reading list:  V. Chvátal: <i>Linear Programming</i>
Recommended previous knowledge: Numerical Mathematics I, Algorithmic programming
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Numerics

Multigrid and split and merge technique (Multigrid und Gebietszerlegung)			A
Type of course	SWS	Credit points:	Responsibility
Bachelor and Master	2+1	5	IFAM
Regularity: regularly every 1-2 years			
Course overview: <ul style="list-style-type: none"> • Preconditioned iterative methods (Richardson, Jacobi) • Multigrid (for finite difference and finite element methods) • Multilevel methods (additive and multiplicative Schwarz methods) • Domain decomposition methods (Schwarz alternating method) 			
Reading list:  Standard literature, lecture notes			
Recommended previous knowledge: Numerical Mathematics I			
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Numerics 			


Nonlinear optimization I (Nichtlineare Optimierung I)			A
Type of course	SWS	Credit points:	Responsibility
Bachelor and Master	4+2	10	Steinbach
Regularity: regularly every 2-3 years			
Course overview: <ul style="list-style-type: none"> • Steepest descent method, Newton's method, line search, trust region • Theory of constrained optimization: KKT conditions, ... • Quadratic optimization: KKT factorizations, active set method • Maratos effect, merit functions, SQP method 			
Reading list:  J. Nocedal, S. Wright: <i>Numerical Optimization</i> , 2nd ed.			
Recommended previous knowledge: Numerical Mathematics I and II, Algorithmic programming			


Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Numerics

Nonlinear optimization II (Nichtlineare Optimierung II)			A
Type of course Bachelor and Master	SWS 4+2	Credit points 10	Responsibility Steinbach
Regularity: regularly every 2-3 years			
Course overview: <ul style="list-style-type: none"> • Nonlinear CG method • Techniques for high dimension models • Interior point methods • Further topics 			
Reading list:  J. Nocedal, S. Wright: <i>Numerical Optimization</i> , 2 nd ed.			
Recommended previous knowledge: Nonlinear optimization I			
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Numerics 			

Numerics for contact problems (Numerik für Kontaktprobleme)			A
Type of course Bachelor and Master	SWS 2+1	Credit points: 5	Responsibility IFAM
Regularity: regularly every 1-2 years			
Course overview: <ul style="list-style-type: none"> • Existence and uniqueness of solutions for elliptic contact problems • Variational inequalities, mixed formulations • Penalty methods • Iterative algorithms: Uzawa, Semi-smooth Newton's method • Multifield problems (Mehrfeldprobleme), coupling with heat equation 			
Reading list:  Standard literature, lecture notes			
Recommended previous knowledge: Numerical Mathematics I			
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Numerics 			

Numerics Partial Differential Equations (Numerik partieller Differentialgleichungen)			A
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility IFAM
Regularity: regularly every 1-2 years			

<p>Course overview:</p> <ul style="list-style-type: none"> • Galerkin method for elliptic boundary value problems • Finite element spaces • A-posteriori error estimation • Methods for parabolic and hyperbolic differential equations <p>Reading list:</p> <p> P. Knabner, L. Angermann: <i>Numerik partieller Differentialgleichungen</i></p> <p>Recommended previous knowledge: Numerical Mathematics I and II</p> <p>Module affiliation:</p> <ul style="list-style-type: none"> • Specialization Bachelor Numerics

Theory of approximation procedure (Theorie der Näherungsverfahren)			A
Type of course	SWS	Credit points:	Responsibility
Bachelor and Master	2+1	5	IFAM
Regularity: regularly every 1-2 years			
<p>Course overview:</p> <ul style="list-style-type: none"> • Error analysis for projection methods • Hilbert spaces, Sobolev spaces • Ritz method, lemmas of Lax-Milgram and Céa, general projection method, Babuska-Brezzi conditions • Applications in FEM (and BEM?) <p>Reading list:</p> <p> Standard literature, lecture notes</p> <p>Recommended previous knowledge: Numerical Mathematics I</p> <p>Module affiliation:</p> <ul style="list-style-type: none"> • Specialization Bachelor Numerics 			

B.6 Differentialgeometrie

Analysis auf Mannigfaltigkeiten			R
Art der Vorlesung Master und GRK	SWS 4+2	Credit points: 10	Verantwortung IDG
Regelmäßigkeit: unregelmäßig			
Inhalt: Sobolev-Theorie auf Mannigfaltigkeiten, isoperimetrische Ungleichungen, Laplace-, Cauchy-Riemann- und Dirac-Operatoren, Wärmeleitungskerne, Greensche Funktionen, Vergleichssätze für den Laplace-Operator und Wärmeleitungskern, Volumenwachstum, Harnack-Ungleichungen, Spektraltheorie.			
Empfohlene Vorkenntnisse: Differentialgeometrie/Globale Analysis			

Eichfeldtheorie			R
Art der Vorlesung Master und GRK	SWS 4+2	Credit points: 10	Verantwortung IDG
Regelmäßigkeit: unregelmäßig			
Inhalt: Zusammenhänge auf Hauptfaserbündeln und deren Krümmung, Eichtransformationen, Yang-Mills-Funktional und Yang-Mills-Gleichung, selbstduale und invariante Zusammenhänge, nichtminimale Yang-Mills-Zusammenhänge, magnetische Monopole und Wirbel			
Empfohlene Vorkenntnisse: Differentialgeometrie/Globale Analysis			

Klassische Differentialgeometrie			R
Art der Vorlesung Bachelor, Master und GRK	SWS 4+2	Credit points: 10	Verantwortung IDG
Regelmäßigkeit: unregelmäßig			
Inhalt: <ul style="list-style-type: none"> • Kurven: Bogenlänge, Krümmung und Torsion, Hauptsatz, Windungszahl, Umlaufzahl, Hopfscher Umlaufsatz, isoperimetrische Ungleichung, Vierscheitelsatz, Frenet-Kurven, Satz von Fenchel • Flächen: reguläre Flächen, Parameterwechsel, Tangentialraum, Differential, erste Fundamentalform, Orientierbarkeit, Gauß-Abbildung, Weingarten-Abbildung, zweite Fundamentalform, Hauptkrümmungen, mittlere Krümmung, Gauß-Krümmung • Innere und äußere Geometrie: Isometrien, Vektorfelder und kovariante Ableitung, Christoffel-Symbole, Koszul-Formel, Krümmungstensor, Gauß-Gleichungen, TheoremaEgregium, Geodätische, Exponentialabbildung, geodätische Polarkoordinaten, Gauß-Lemma, sphärische und hyperbolische Geometrie 			
Empfohlene Vorkenntnisse:			
Module affiliation: <ul style="list-style-type: none"> • Grundlagen und Spezialisierung Bachelor Geometrie 			

Elliptische Differentialgleichungen aus der Geometrie			R
Art der Vorlesung Bachelor, Master und GRK	SWS 4+2	Credit points: 10	Verantwortung IDG
Regelmäßigkeit: unregelmäßig			
Inhalt: <ul style="list-style-type: none"> • elliptische Differentialgleichungen auf Mannigfaltigkeiten • harmonische Abbildungen und Schnitte in Vektorraumbündeln • Minimalflächen und das Bernstein-Problem • Yamabe-Problem • Mannigfaltigkeiten vorgeschriebener Krümmung • Yang-Mills-Gleichungen • Existenz- und Eindeutigkeitsfragen • Regularitätstheorie 			
Empfohlene Vorkenntnisse:			
Module affiliation: <ul style="list-style-type: none"> • Spezialisierung Bachelor Geometrie 			

Geometrische Evolutionsgleichungen			R
Art der Vorlesung Master und GRK	SWS 4+2	Credit points: 10	Verantwortung IDG
Regelmäßigkeit: unregelmäßig			
Inhalt: Parabolische Differentialgleichungen auf Mannigfaltigkeiten, Variationsprobleme, Wärmeleitungsgleichung, mittlerer Krümmungsfluss, Ricci-Fluss, harmonischer Wärmefluss, Yamabe- und Yang-Mills-Flüsse, Fragen zur Langzeitexistenz und Konvergenz, Maximumprinzipien für Tensoren, geometrische Harnack-Ungleichungen			
Empfohlene Vorkenntnisse:			

Komplexe Differentialgeometrie			R
Art der Vorlesung Bachelor, Master und GRK	SWS 4+2	Credit points: 10	Verantwortung IDG
Regelmäßigkeit: alle ein bis drei Jahre, Wintersemester			
Inhalt: Komplexe Mannigfaltigkeiten, fast komplexe Strukturen, Nijenhuis-Tensor und Integrabilität, fast hermitesche Mannigfaltigkeiten, Klassifikation nach Gray-Hervella, Kähler-Mannigfaltigkeiten, Dolbeault-Operatoren, Zerlegungssatz von Dolbeault, Hodge-Zahlen, Serre-Dualität, Chern-Klassen, -Formen und -Zahlen, Satz von Gauß-Bonnet-Chern, Calabi-Vermutung und der Beweis von Yau, Calabi-Yau-Mannigfaltigkeiten			
Empfohlene Vorkenntnisse: Differentialgeometrie/Globale Analysis, Funktionentheorie			

Module affiliation: <ul style="list-style-type: none"> Wahlmodule Bachelor und Master Mathematik
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Konforme Geometrie			R
Art der Vorlesung Bachelor, Master und GRK	SWS 4+2	Credit points: 10	Verantwortung IDG
Regelmäßigkeit: unregelmäßig			
Inhalt: Konforme Abbildungen, stereographische und Mercator-Projektion, konforme Gruppe des euklidischen Raumes und der Sphäre, der Satz von Liouville, Möbius-Transformationen und deren Klassifikation, Beziehungen zur projektiven und hyperbolischen Geometrie, Fuchssche und Kleinsche Gruppen, konforme Geometrie von Flächen, Uniformisierung			
Empfohlene Vorkenntnisse:			
Module affiliation: <ul style="list-style-type: none"> Wahlmodule Bachelor und Master Mathematik 			

Riemannsche Geometrie			R
Art der Vorlesung Bachelor, Master und GRK	SWS 4+2	Credit points: 10	Verantwortung IDG
Regelmäßigkeit: alle ein bis drei Jahre, Wintersemester			
Inhalt: Riemannsche Metriken, Geodäten, Exponentialabbildung, Injektivitätsradius, Krümmung eines Zusammenhangs, erste und zweite Variation der Energie einer Kurve, Existenz geschlossener Geodäten, Satz von Synge, konjugierte Punkte, Jacobi-Felder, Vergleichssätze von Rauch, symmetrische und lokal symmetrische Räume			
Empfohlene Vorkenntnisse: : Differentialgeometrie/Globale Analysis,			
Module affiliation: <ul style="list-style-type: none"> Wahlmodule Bachelor und Master Mathematik 			


Spin-Geometrie			R
Art der Vorlesung Bachelor, Master und GRK	SWS 4+2	Credit points: 10	Verantwortung IDG
Regelmäßigkeit: unregelmäßig			

Inhalt: Clifford-Algebra, Spin-Gruppe, Spin-Darstellung, Clifford-Multiplikation, Spin-Strukturen und Spinor-Bündel, Dirac-Operator, Lichnerowicz-Formel und Eigenwertabschätzungen, Killing- und Twistor-Spinoren
Empfohlene Vorkenntnisse:
Module affiliation: <ul style="list-style-type: none"> Wahlmodule Bachelor und Master Mathematik


Symplektische Geometrie			R
Art der Vorlesung Bachelor, Master und GRK	SWS 4+2	Credit points: 10	Verantwortung IDG
Regelmäßigkeit: unregelmäßig			
Inhalt: Symplektische Vektorräume, symplektische und Lagrange-Unterräume, symplektische Basis, symplektische Mannigfaltigkeiten, Kotangentialbündel und koadjungierte Orbits als symplektische Mannigfaltigkeiten, Mosers Trick und der Satz von Darboux, Hamilton-Vektorfelder und Poisson-Klammer, Hamiltonsche Wirkungen und Impulsabbildung, Kapazitäten, pseudoholomorphe Kurven, Modelle der klassischen Mechanik, Legendre-Transformation, symplektische Hodge-Theorie, symplektische Zusammenhänge			
Empfohlene Vorkenntnisse:			
Module affiliation: <ul style="list-style-type: none"> Wahlmodule Bachelor und Master Mathematik 			


Transformationsgruppen			R
Art der Vorlesung Bachelor, Master und GRK	SWS 4+2	Credit points: 10	Verantwortung IDG
Regelmäßigkeit: unregelmäßig			
Inhalt: Lie-Gruppen, Lie-Algebra, Exponentialabbildung, Struktur nilpotenter, auflösbarer und halbeinfacher Lie-Algebren, Gruppenwirkungen, G-Strukturen, Kleinsches Erlanger Programm, homogene Räume, fundamentale Vektorfelder, adjungierte Darstellungen, reduktive homogene Räume, symmetrische Räume und deren Klassifikation			
Empfohlene Vorkenntnisse:			
Module affiliation: <ul style="list-style-type: none"> Wahlmodule Bachelor und Master Mathematik 			



B.7 Mathematical Stochastics




Asymptotic Statistics (Asymptotische Statistik)			A
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility N.N.
Regularity: irregular			
<p>Course overview:</p> <ul style="list-style-type: none"> • contiguous distributions • local asymptotic normality • limit experiments • asymptotically optimal tests • asymptotic efficiency of estimators and tests • contiguous distributions • local asymptotic normality • limit experiments • asymptotically optimal tests • asymptotic efficiency of estimators and tests <p>Reading list:</p> <p> Van der Vaart: <i>Asymptotic Statistics</i>, Cambridge University Press, Cambridge, 1998.</p> <p>Recommended previous knowledge: Probability and Statistics II</p> <p>Module affiliation:</p> <ul style="list-style-type: none"> • Specialization Bachelor Stochastics • Master elective module 			

Financial Mathematics in Discrete Time (Finanzmathematik in diskreter Zeit)			A
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility Weber
Regularity: annual			


<p>Course overview:</p> <ul style="list-style-type: none"> • Arbitrage Pricing Theory • Preferences and Utility • Optimality and Equilibrium • Risk Measures <p>Reading list:</p> <p> H. Föllmer & A. Schied: <i>Stochastic Finance</i>, de Gruyter, Berlin/New York, 2016.</p> <p>Recommended previous knowledge: Probability and Statistics II</p>
<p>Module affiliation:</p> <ul style="list-style-type: none"> • Specialization Bachelor Stochastics • Master elective module



Financial Mathematics in Continuous Time (Finanzmathematik in stetiger Zeit)			A
Type of course	SWS	Credit points: 10	Responsibility
Bachelor and Master	4+2		Weber
Regularity: annual			
<p>Course overview:</p> <ul style="list-style-type: none"> • Introduction to Stochastic Analysis • Financial Mathematics in Continuous Time: Pricing and Hedging of Financial Derivatives (Equity Derivatives, Interest rate Derivatives, and Credit Derivatives), Optimal Investment <p>Reading list:</p> <p> M. Musiela & R. Rutkowski: <i>Martingale Methods in Financial Modelling</i>, Springer, 2005.</p> <p>Recommended previous knowledge: Probability and Statistics II, Financial Mathematics in Discrete Time</p>			
<p>Module affiliation:</p> <ul style="list-style-type: none"> • Specialization Bachelor Stochastics • Master elective module 			

Financial Mathematics: New Developments (Finanzmathematik: Aktuelle Entwicklungen in der Finanzmathematik)			A
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility Weber
Regularity: irregular			
Course overview: <ul style="list-style-type: none"> New Directions in Financial Mathematics 			
Reading list: <ul style="list-style-type: none">  M. Musiela& R. Rutkowski: <i>Martingale Methods in Financial Modelling</i>, Springer, 2005.  H. Föllmer& A. Schied: <i>Stochastic Finance</i>, de Gruyter, Berlin/New York, 2016. 			
Recommended previous knowledge: Probability and Statistics II, Financial Mathematics in Discrete Time, Financial Mathematics in Continous Time			
Module affiliation: <ul style="list-style-type: none"> Specialization Bachelor Stochastics Master elective module 			



Markov Chains (Markov-Ketten)				A
Type of course Bachelor and Master	SWS 2+1	Credit points: 5	Responsibility Grübel	
Regularity: irregular				
Course overview: Markov chains are stochastic processes with the property that the future development depends on the history sofar only via the present state (lack of memory). They are important in a great variety of applications, such as server systems, communication networks, analysis of algorithms and in the context of combinatorial optimization. Only finite or countably infinite state spaces are considered, which means that only a limited amount of measure theory is needed. In particular, this course is also suitable for students who aim for a career as school teachers.				
Reading list: <ul style="list-style-type: none">  Bremaud, P.: Markov Chains. Springer, 1999  Levin, D.A., Peres, Y., Wilmer, E.L.: Markov Chains and Mixing Times  American Mathematical Society, 2009 				
Recommended previous knowledge: Probability and Statistics I				
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Stochastics • Master elective module 				


Nonparametric Statistics (Nichtparametrische Statistik)				A
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility N.N.	
Regularity: irregular				

<p>Course overview:</p> <ul style="list-style-type: none"> • order and rank statistics • distribution free confidence regions • locally best rank tests • empirical distributions • tests for goodness of fit • nonparametric multivariate procedures <p>Grundlegende Literatur:</p> <p> J. Hajek, Z. Sidak, P. K. Sen: <i>Theory of Rank Tests</i>, Academic Press, 1999.</p> <p>Recommended previous knowledge: Probability and Statistics II</p> <p>Module affiliation:</p> <ul style="list-style-type: none"> • Specialization Bachelor Stochastics • Master elective module

Life Insurance Mathematics (Personenversicherungsmathematik)			A
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility Weber
Regularity: annual			
<p>Course overview:</p> <ul style="list-style-type: none"> • Interest Rates and Fixed Income • Cash Flows and the Mathematical Reserve • Difference Equations and Differential Equations • Hattendorff's Theorem • Unit-Linked Policies • Policies with Stochastic Interest Rate • Market-Consistent Valuation <p>Reading list:</p> <p> M. Koller: <i>Stochastic Models in Life Insurance</i>, Springer, 2012.</p> <p> R. Norberg: <i>Basic Life Insurance Mathematics</i>, LSE, 2002.</p>			

Recommended previous knowledge: Probability and Statistics II
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Stochastics • Master elective module

Non-Life Insurance Mathematics (Schadenversicherungsmathematik)			A
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility Weber
Regularity: annual			
Course overview: <ul style="list-style-type: none"> • Risk Modelling • Ruin Theory • Premium Calculation, Tariffication and Generalized Linear Models • Claim Reserving • Reinsurance 			
Reading list: <ul style="list-style-type: none">  T. Mack: <i>Schadenversicherungsmathematik</i>, VVW Karlsruhe, 2002.  K. Schmidt: <i>Versicherungsmathematik</i>, Springer, 2006. 			
Recommended previous knowledge: Probability and Statistics II			
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Stochastics • Master elective module 			

Game Theory (Spieltheorie)			A
Type of course Bachelor and Master	SWS 2+1	Credit points: 5	Responsibility N.N.
Regularity: irregular			
Course overview: <ul style="list-style-type: none"> • normal form of n-person games • points of equilibrium • mixed extensions • two-person zero sum games • minimax theorems and minimax strategies • matrix games • cooperative games • Shapley value 			
Reading list: <ul style="list-style-type: none"> •  F. Forgo, J. Szep, F. Szidarovszky: <i>Introduction to the Theory of Games: Concepts, Methods, Applications</i>, Kluwer, Dordrecht, 1999. 			
Recommended previous knowledge: Probability and Statistics II			
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Stochastics • Master elective module 			

Statistical Decision Theory and Sequential Procedures (Statistische Entscheidungstheorie und Sequentialverfahren)			A
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility N.N.
Regularity: irregular			
Course overview: <ul style="list-style-type: none"> • decision kernels • Bayes and minimax procedures for estimation and testing • minimax theorems • optimal stopping • sequential Bayes procedures • sequential likelihood ratio tests • optimal sequential tests 			
Reading list: <ul style="list-style-type: none"> 📖 Irle: <i>Sequentialanalyse: Optimale sequentielle Tests</i>, Teubner, Stuttgart, 1990. 📖 H. Strasser: <i>Mathematical Theory of Statistics</i>, de Gruyter, Berlin, 1985. 			
Recommended previous knowledge: Probability and Statistics II			
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Stochastics • Master elective module 			


Statistics (Statistische Verfahren)			A
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility Grübel, N.N.
Regularity: irregular			
Course overview: <ul style="list-style-type: none"> • tests for goodness of fit, bootstrap, density estimation, robust procedures • models with covariates: regression, analysis of variance, generalized linear models 			
Reading List: <ul style="list-style-type: none"> 📖 W. N. Venables und B. D. Ripley: <i>Modern Applied Statistics with S-Plus</i>, third edition. Springer, New York, 1999. 			

Recommended previous knowledge: Probability and Statistics I and II
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Stochastics • Master elective module

Stochastic Analysis (Stochastische Analysis)			A/R
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility IfMS
Regularity: annual			
Course overview: <ul style="list-style-type: none"> • Stochastic Processes in Continuous Time: Brownian Motion, (Local) Martingales, Semimartingales, Markovian Processes, Levy Processes • stochastic Integrals • Representations of Martingales • Girsanov's and its Applications • Stochastic Differential Equations • Applications to Financial Mathematics 			
Reading list: <ul style="list-style-type: none"> 📖 P. Protter: <i>Stochastic Integration and Differential Equations</i>, Springer, 2005 📖 D. Revuz, M. Yor: <i>Continuous Martingales and Brownian Motion</i>, Springer, 1999. 📖 L. C. G. Rogers, D. Williams: <i>Diffusions, Markov Processes and Martingales</i>, Volumes 1 & 2, Wiley, New York, 1987, 1994. 			
Recommended previous knowledge: Probability and Statistics II			

Module affiliation:

- Specialization Bachelor Stochastics
- Master elective module

Stochastic Methods of Operations Research (Stochastische Methoden des Operations Research)			A
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility N.N.
Regularity: irregular			
Course overview:			
<ul style="list-style-type: none"> • Markov chains • martingales • renewal theory • regenerative processes • queueing theory 			
Reading list:			
 Asmussen, S., Applied Probability and Queues, Wiley, New York, 2003.			
Recommended previous knowledge: Probability and Statistics II			
Module affiliation:			
<ul style="list-style-type: none"> • Specialization Bachelor Stochastics • Master elective module 			

Stochastic Simulation (Stochastische Simulation)			A
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility Grübel, N.N.
Regularity: irregular			
Course overview: <ul style="list-style-type: none"> • generation of and tests for pseudo random numbers • methods for non-uniform distributions • variance reduction and rare event simulation • Monte Carlo integration • MCMC (Markov Chain Monte Carlo) • applications to combinatorial optimization, Operations Research, insurance mathematics and finance 			
Reading list: <ul style="list-style-type: none"> 📖 S. Asmussen und Glynn, W. Peter: <i>Stochachstic Simulation Algorithms and Analysis</i>, Springer, New York, 2007. 📖 P. Bratley, B. Fox und L. Schrage: <i>A Guide to Simulation</i>, Springer, New York, 1983. 			
Recommended previous knowledge: Probability and Statistics I and II			
Module affiliation: <ul style="list-style-type: none"> • Specialization Bachelor Stochastics • Master elective module 			

Random Structures and Algorithms (Zufällige diskrete Strukturen und Algorithmen)			A/R
Type of course Bachelor and Master	SWS 4+2	Credit points: 10	Responsibility Grübel
Regularity: irregular			

Course overview:

- structure of random permutations and partitions
- binary and plane trees, algorithms for sorting and searching
- random graphs


Reading list:

- 📖 S. Janson, T. Luczak, A. Rucinski: *Random Graphs*, Wiley, New York, 2000.
- 📖 R. Motwani, P. Raghavan: *Randomized Algorithms*, Cambridge University Press, Cambridge, 1995.
- 📖 J. Pitman: *Combinatorial Stochastic Processes*, Lecture Notes in Mathematics. Springer, New York, 2006.

Recommended previous knowledge: Probability and Statistics I and II

Module affiliation:

- Specialization Bachelor Stochastics
- Master elective module

Time Series Analysis (Zeitreihenanalyse)			A
Type of course	SWS	Credit points:	Responsibility
Bachelor and Master	2+1	5	N.N.
Regularity: irregular			
Course overview:			
<ul style="list-style-type: none"> • stationary time series • autocovariance function and spectral measure • autoregressive processes, moving average processes • spectral representation • Kolmogorov's prediction theory • Statistics in the time domain (estimators for the mean and covariance function) • Statistics in the frequency domain (periodogram, estimators for the spectral density) 			
Reading list:			
 J.-P. Kreiß, G. Neuhaus: <i>Einführung in die Zeitreihenanalyse</i> , Springer, Berlin, 2006.			
Recommended previous knowledge: Probability and Statistics II			
Module affiliation:			
<ul style="list-style-type: none"> • Specialization Bachelor Stochastics 			